# Deep Equilibrium Model for Memory Efficient Stereo Matching on the High Resolution Argoverse Dataset

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# 1. Introduction

The estimation of depth from stereo image pairs is a longstanding computer vision task with applications in robotics [12, 13]. In this report, we are interested in building a stereo matching solution for a high resolution images in the Argoverse dataset [8] that runs within 200ms in modern GPUs. To allow for flexible design of the model in satisfying the time requirements, we adopt a RAFT based model in our solution [16, 18] which has gained much attention [6, 14] in recent years, wherein an update operation is iteratively performed to refine the disparity predictions as well as the hidden states. Through the use of such design, the number of unrolled iterations can be adjusted depending on the desired model latency.

However, this class of models also introduces huge memory consumption necessary for backpropagation through time (BPTT) during training. To address this issue, We introduce the following contributions. First, we adopt deep equilibrium (DEQ) formulation [2, 3] into our RAFT-based stereo model. Additionally, to improve the representation power, we follow the canonical volumetric based deep stereo models [7, 15] and use 3D convolutions to extract geometric features from the cost volume. This 3D features are utilized during the iterative updates which supplies the network with geometric knowledge. We also utilize the 3D features to regress an initial disparity estimate, allowing for better convergence of the model [4].

# 2. Method

The overall model contains two principal components, the volumetric submodule and the iterative updates to refine the disparity predictions. We illustrate the model in Figure 1.

#### 2.1. Geometric stereo

We begin by extracting feature maps for both the input images  $I \in \mathbb{R}^{H \times W \times 3}$ . We follow RAFT and pass the images into encoder sub-networks, with the objective of extracting matching and context feature maps. Both the left and right input images are passed into the matching sub-network to give

the matching feature maps  $I_L^m, I_R^m \in \mathbb{R}^{h \times w \times c}$ . The context sub-network is only applied to the reference image, which in this case is the left image, and it gives us the initial hidden states  $h^{[0](s)}$  and the context features  $q^{(s)}$  at multiple scales *s*. We build a cost volume  $\mathbf{C} \in \mathbb{R}^{h \times w \times D \times c_o}$ , following previ-

We build a cost volume  $\mathbf{C} \in \mathbb{R}^{h \times w \times D \times c_o}$ , following previous stereo matching works by computing pairwise correlations [17] using the extracted matching feature maps, where D is the maximum disparity. A 3D UNet is then applied on the correlation volume giving us 3D geometric features  $\mathbf{C}^{(s)} \in \mathbb{R}^{h/2^s \times w/2^s \times D/2^s \times c_s}$  at multiple scales. At the highest scale s = 0 of the aggregated volume, we compute an initial disparity estimate as a weighted sum of the candidate disparities [15]

$$\hat{d_{init}} = \sum_{d=0}^{D} d \times Softmax(q_d).$$
(1)

Alternatively, we use the weighted sum of only the top matching candidates [5].

### 2.2. Deep Equilibrium Stereo

Our iterative updates to refine  $\hat{d}^{[0]}$  and the hidden states  $h^{[0](s)}$  follows the update operations in RAFT-Stereo. A GRU-based [9] convolutional layers are used to update the hidden states using the image contexts  $q^{(s)}$  following the Slow-fast GRU updates. At the highest scale, we additionally sample values from the cost volume that is used as additional input into the update layers. However, instead of sampling just the correlation values from the volumes, we trilinearly sample the 3D features at the disparity of interests, giving our model more representational power that is aware of the 3D contexts.

These update steps, when implemented naively, may consume a massive amount of memory during training, especially with the addition of the 3D contexts on a high resolution input images. Therefore, we adopt a deep equilibrium formulation into our model. Specifically, we solve for the fixed point  $h^{*(s)}$  and  $\hat{d}^*$  and turn off the autograd functionality of Pytorch in all the previous update steps. We also use Anderson solver [1] to accelerate convergence to the fixed



Figure 1. Overall architecture of the model.

point. As the autograd is only turned on at the fixed point, the memory consumption for the iterative updates is reduced to almost free.

The other concern that we need to address is the real-time requirement of the model, and a quick convergence to the fixed point is desirable. The initial disparity predicted by the 3D volumetric sub-network helps with this objective, but we also want to reduce the inference time for the iterative updates. To achieve this, we train a hyper-anderson solver [4] to substitute the traditional anderson solver.

### 3. Experiments

We first train our model on large synthetic datasets before finetuning it to the Argoverse dataset. We use the SceneFlow dataset [17], and also capture a dataset from CARLA driving simulator [10, 11], providing us with a large data in urban driving scenario with sensor configuration which resemble that of Argoverse. We train our model on the synthetic data randomly cropped with size  $512 \times 960$  and a batch size of 4 for 50 epochs. We set the maximum disparity of interest to be 384.

To also improve the generalization ability towards the real world data, we perform color augmentation following [19] by adding random gaussian noise with standard deviation 0.02 and gaussian blur with standard deviation range sampled randomly from [0,1] to the right image. We also apply color jitters to the right image with brightness, contrast, saturation, and hue ranges of 0.2, 0.2, 0.2 and 0.01. Additionally, we perform random zooming and stretching of the image to allow generalization to varying disparity distribution.

We then finetune the model on the Argoverse dataset that is randomly cropped into  $1920 \times 1920$  with a batch size of 2. Training on such a large resolution is made possible due to the DEQ implementation. A hyper anderson solver is then trained with this model as a fixed point target.

Our model is trained on a single Nvidia RTX 3090 GPU. Based on the 200ms and the latency comparison between RTX 3090 and V100, we require our model to run within 200/1.29 = 155ms. In our experiments, we found that we can allow for  $4 \sim 5$  update iterations using the hyper anderson solver. In our submitted result, we only used 4 iterations to ensure our model satisfies the real-time requirements. At the time of submission, this model ranked 2nd on the Argoverse Stereo Competition 2022 Leaderboard.

#### 4. Conclusion

We presented a design of stereo matching network that is flexible to the requirements. The model is inspired by the canonical volumetric design of stereo matching models and the iterative refinements design that is recently gaining attention. By combining both concepts, our model benefits from the geometric knowledge obtained from the volumetric design and the flexibility of iterative refinements. However, more thorough experiments still needs to be done to explore the potential of the proposed model.

The codes will be made available on https://
github.com/antabangun/ges

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